



Improving Stiffness on the A-Axis

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Fabrication Integrated Design Lab

Outline

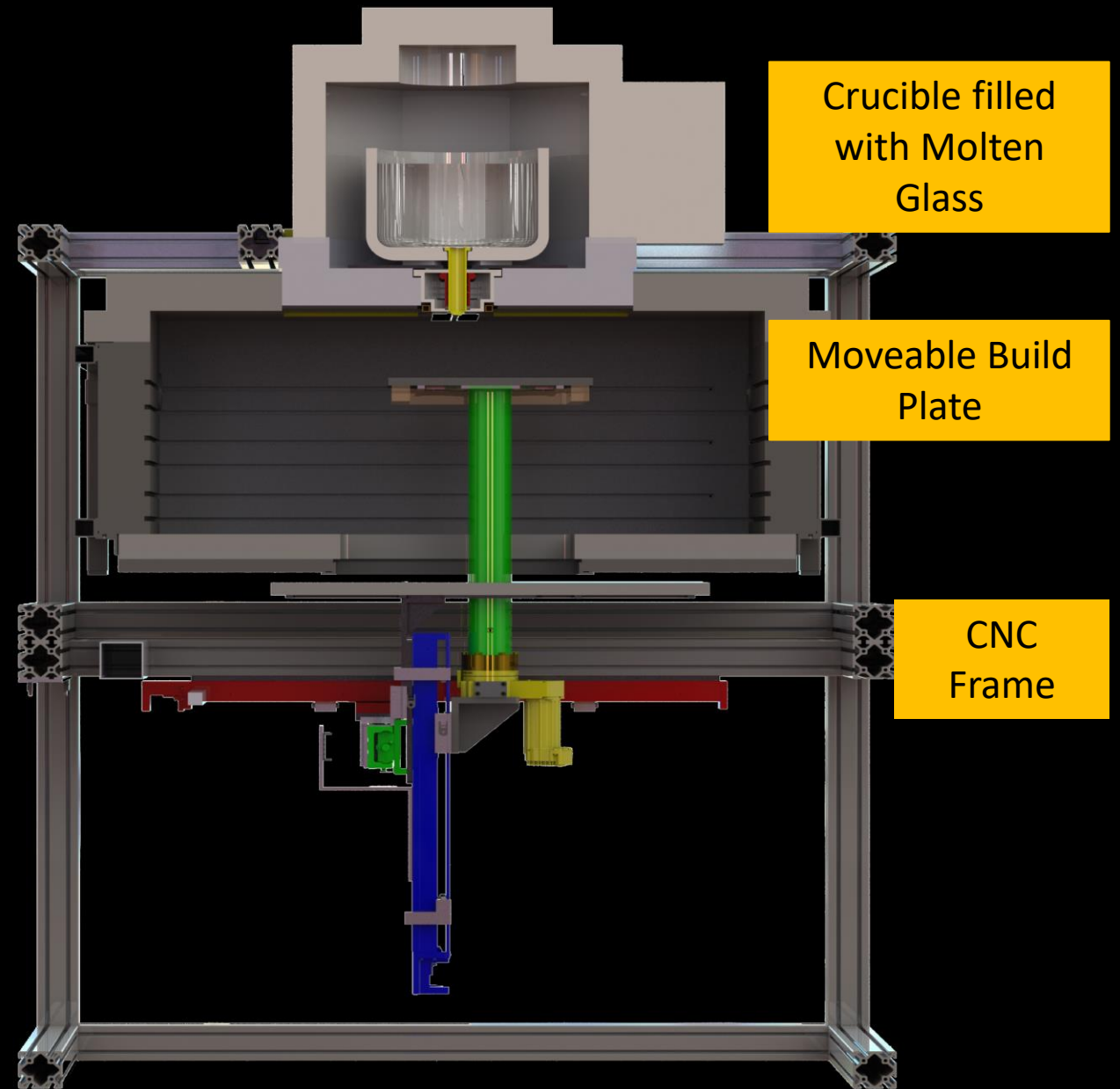
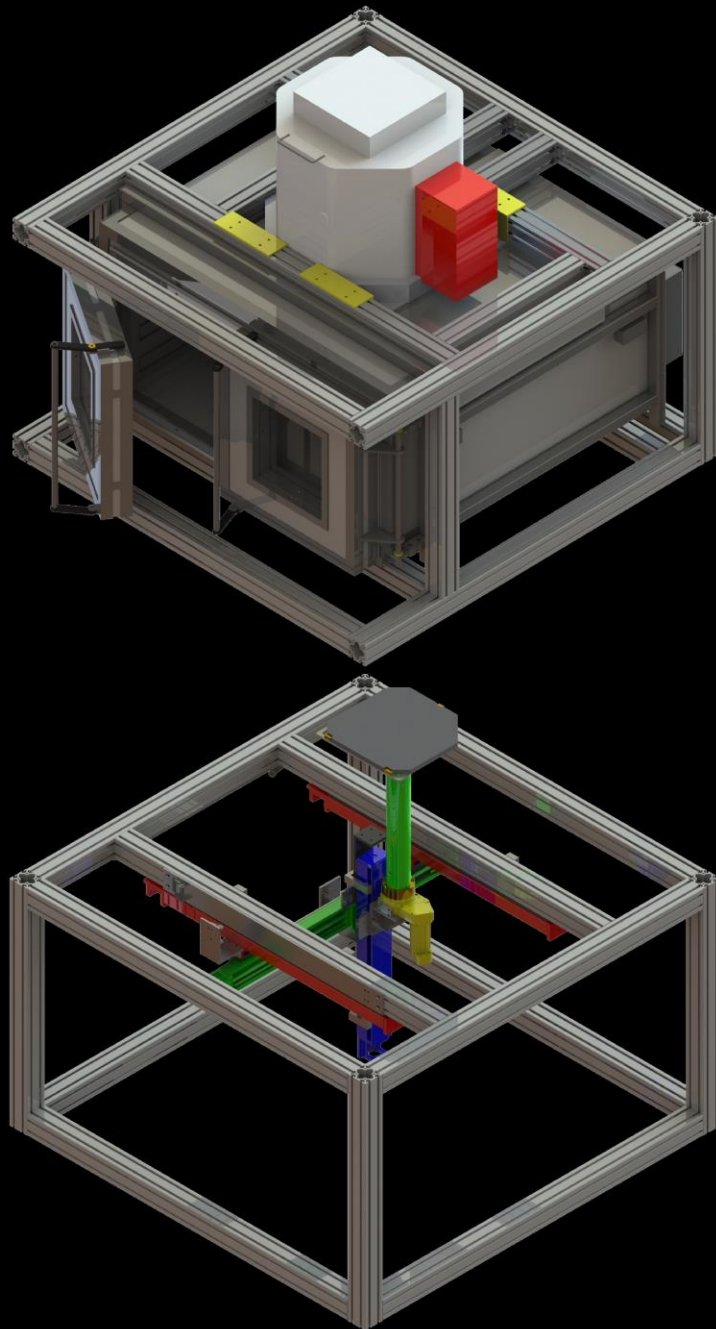
1. Background
2. Problem statement
3. FREDPARRC
4. Machine analysis
5. Failure analysis
6. Design analysis and implementation

Outline

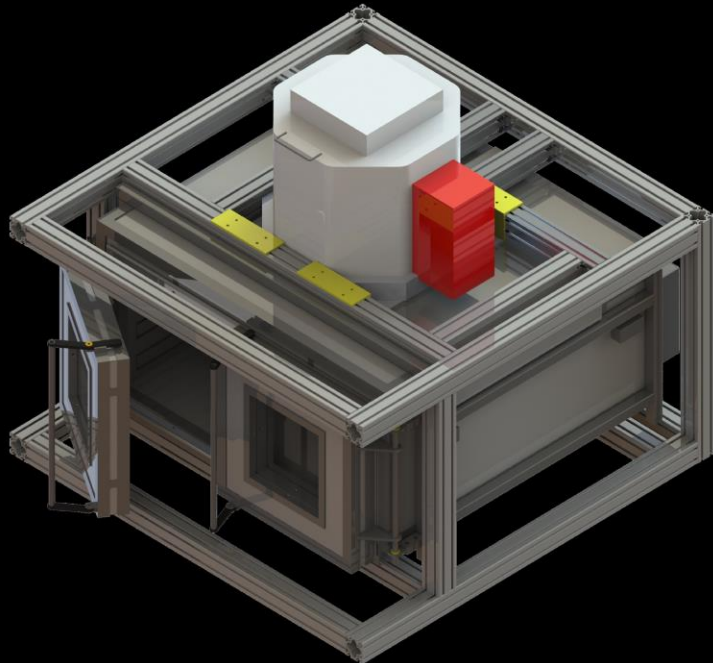
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Glass 3D Printer III

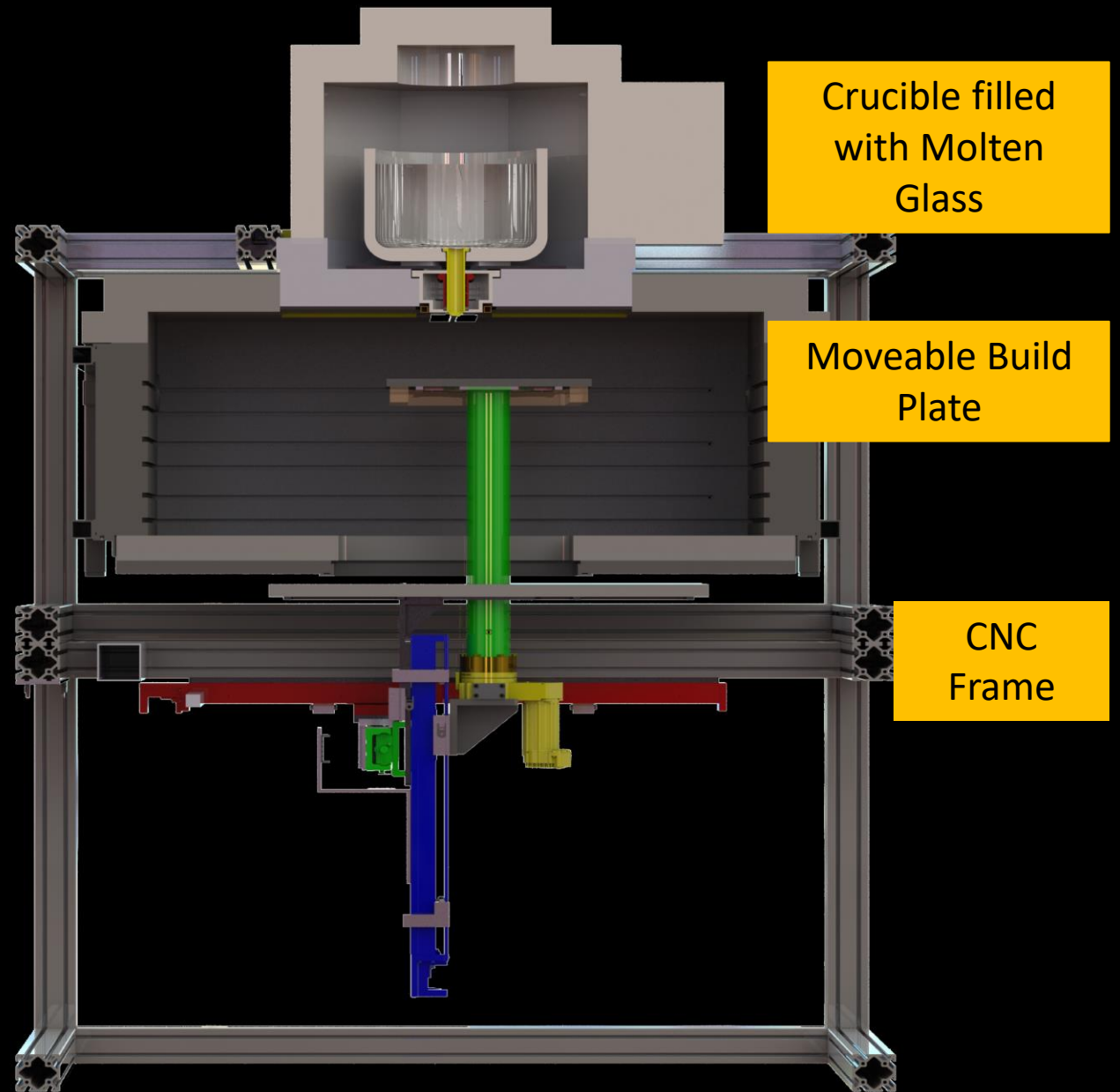
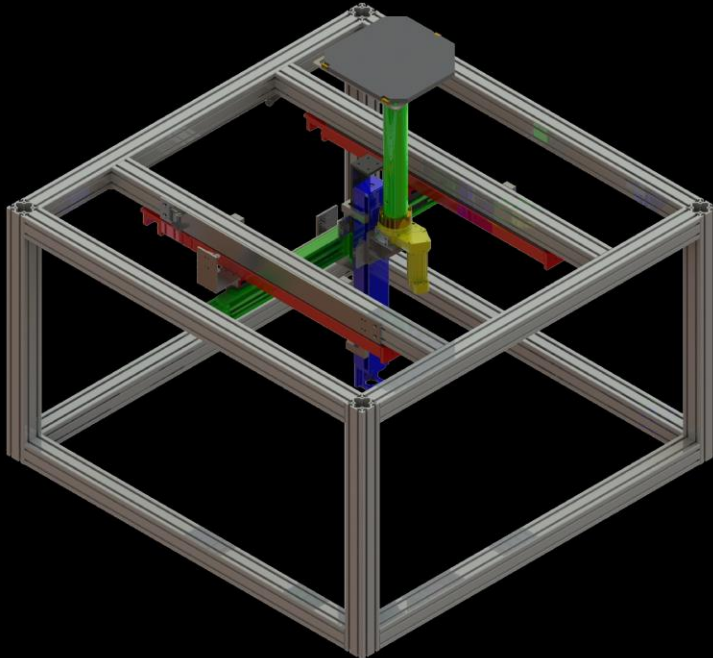




Kiln

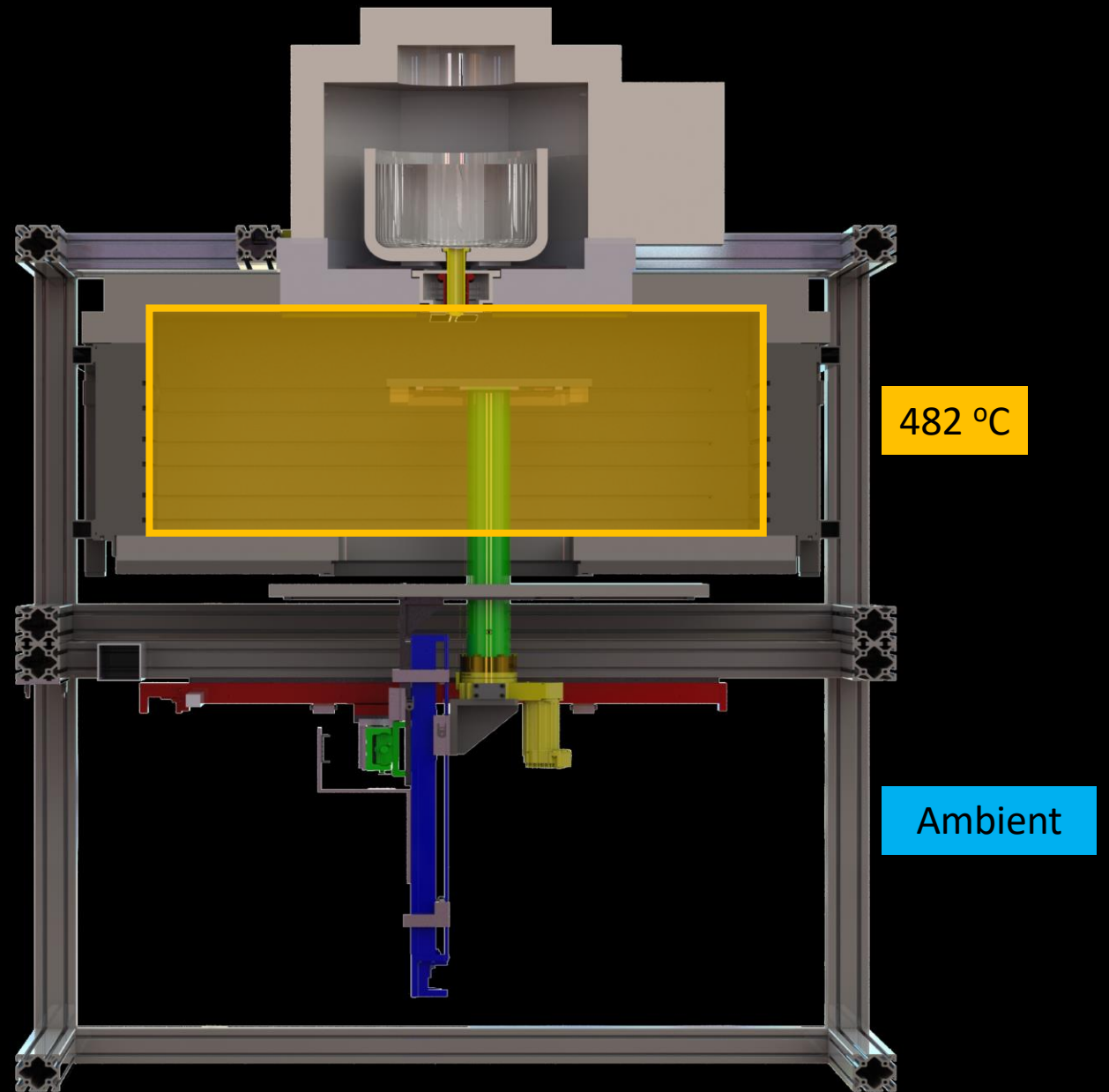


CNC

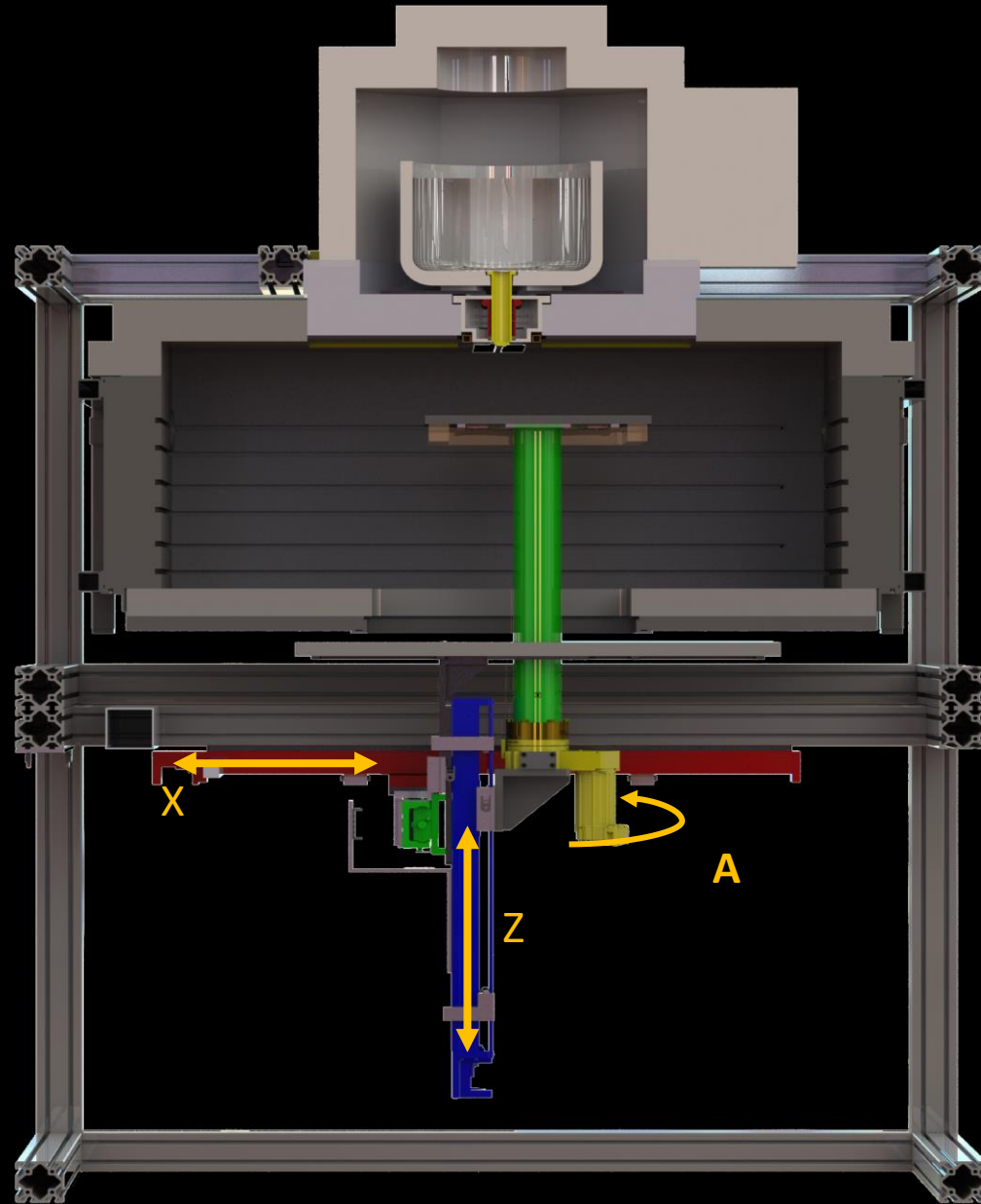
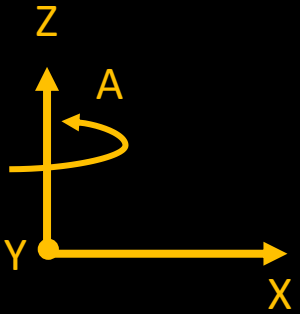




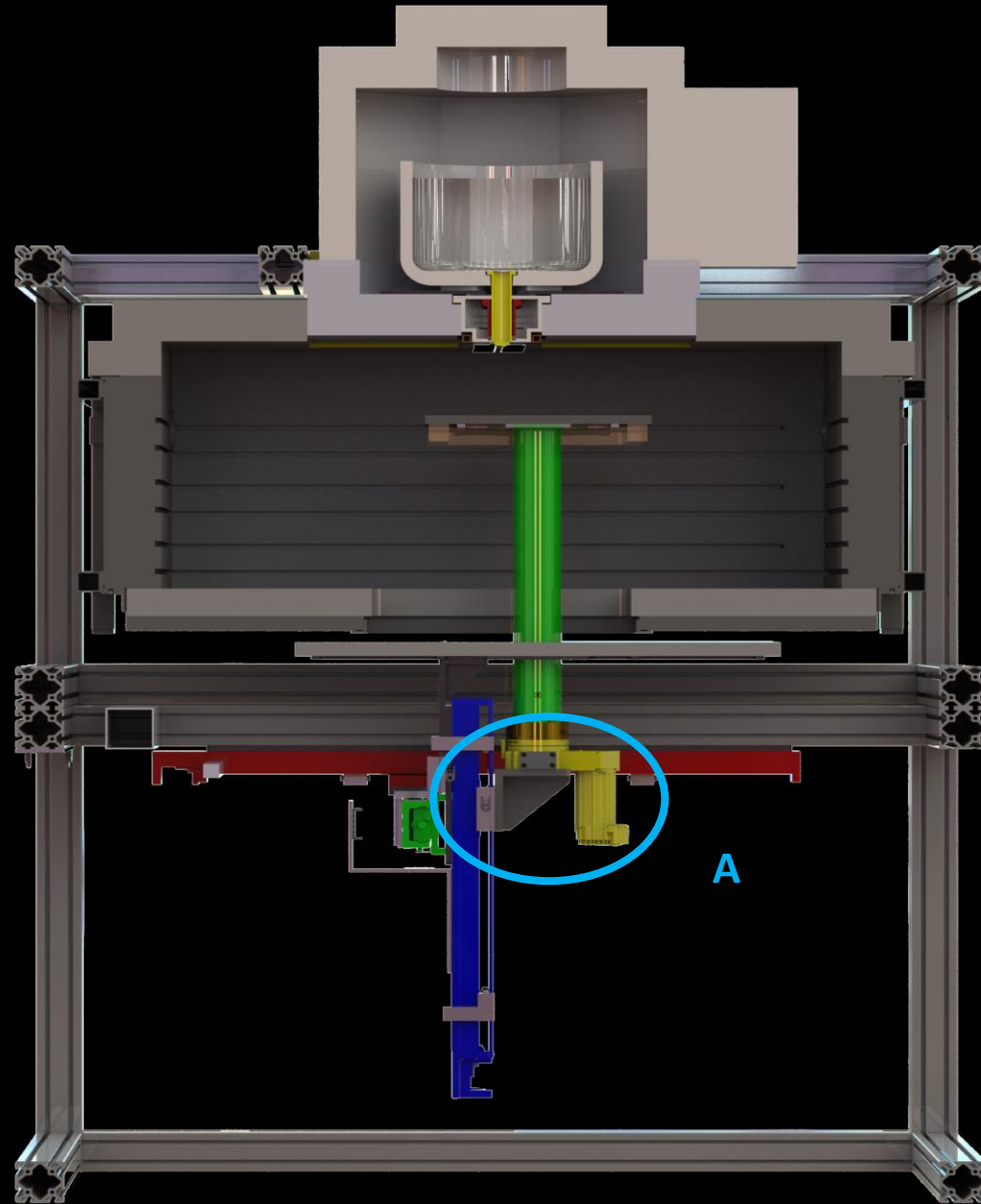
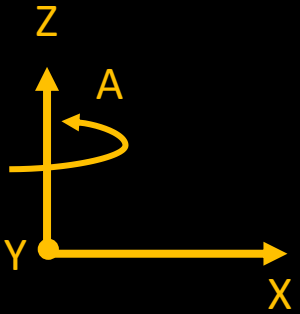
Print Environment



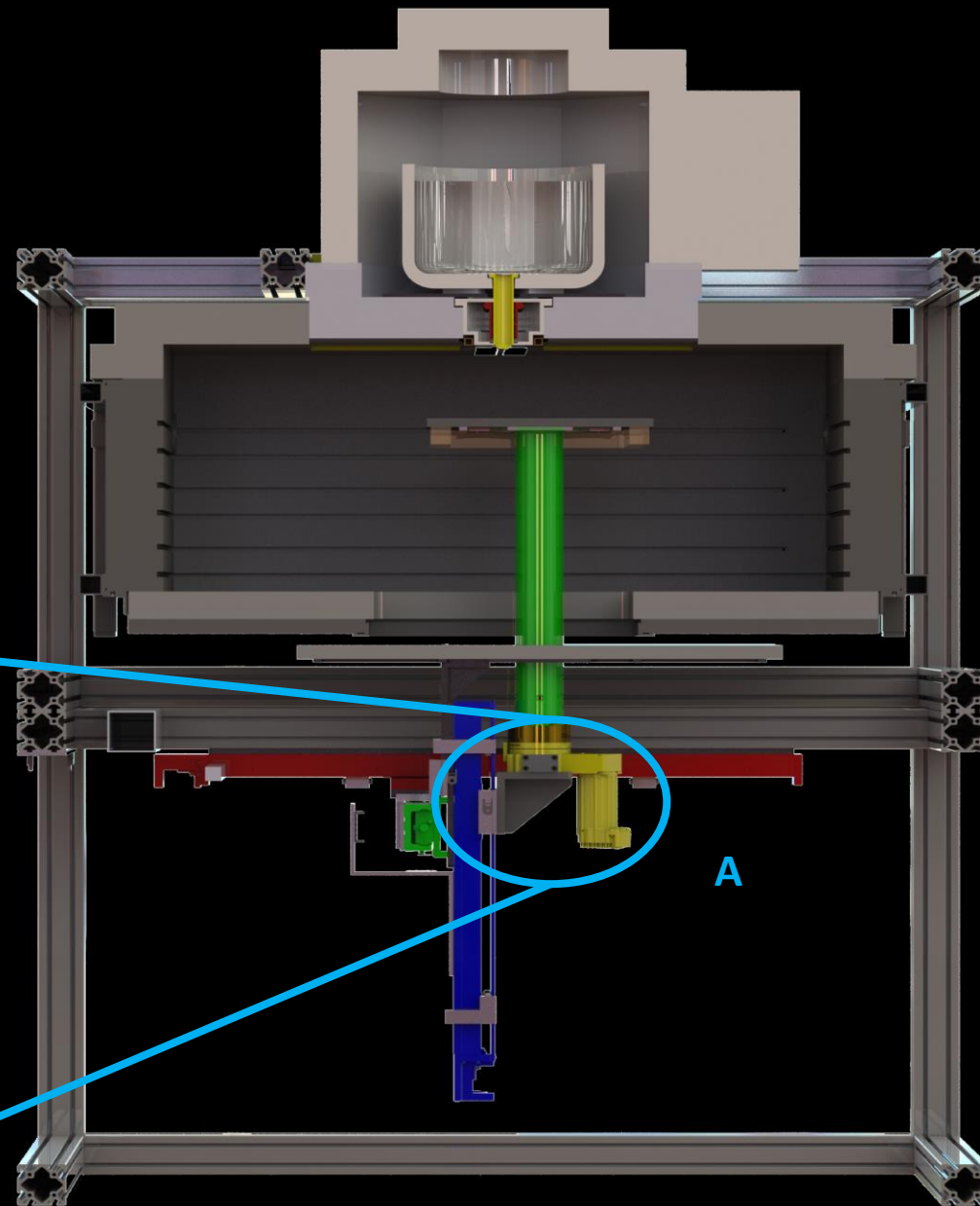
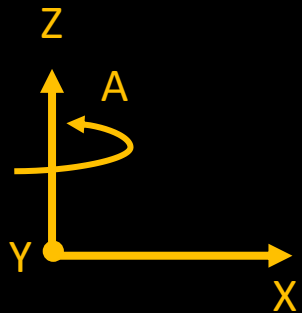
Machine Motion



Project Focus: Rotary Stage



Project Focus 1: Rotary Stage



Bell-Everman SBR-50 Rotary Table

<https://www.bell-everman.com/products/rotary-positioning/servobelt-rotary-stage>

Problem: Low Stiffness on Rotary Stage

Angular deflection at the stage = 1.7 degrees

Estimated horizontal deflection at the build plate = 17 mm

Print accuracy: 0.5 mm₁

Summary of results

Initial Deflection: 17 mm at the build plate

After redesign: 1 mm (calculated)

Less stiff than modeled



Rotary stage with changes



Fully assembled stage

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FREDPARRC

Requirements:

- Return rotary stage to nominal stiffness
- Limit loads to rotary stage below rated levels
- Improve robustness and reliability of machine

Environment:

- Seamless integrate into the existing machine
- 482 °C (annealing oven)
- 30 °C (ambient environment)

FREDPARRC

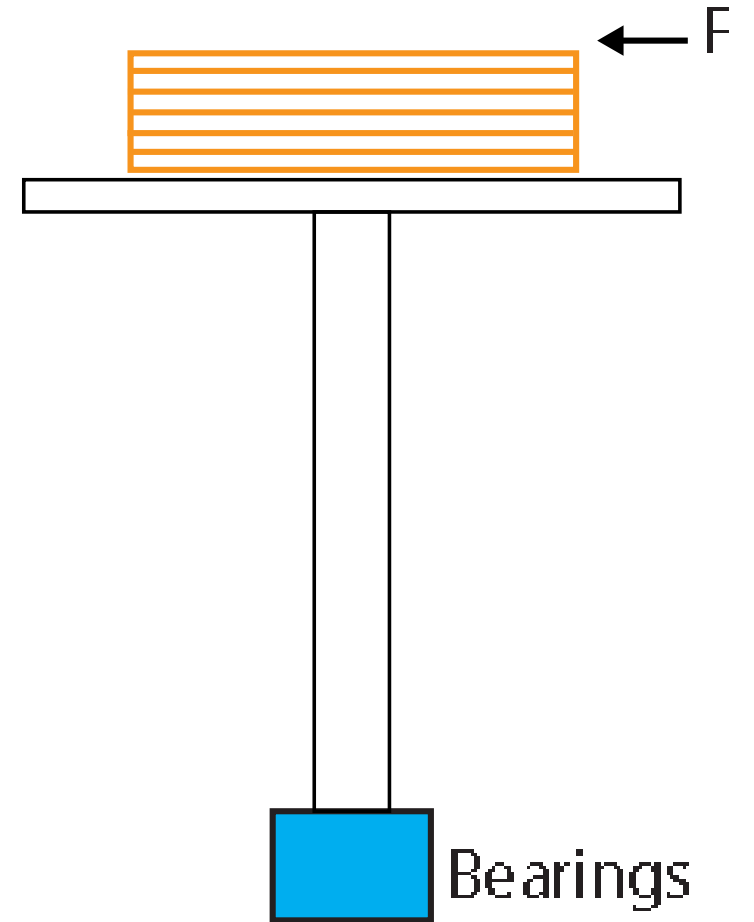
Design Parameters:

- Shaft is 65 cm from build plate to rotary stage
- Load limits for rotary stage:
 - 7.0 kN axially / 4.0 kN radially
 - 120 Nm Torque (200 N lateral force at the build plate)
- Motor torque limits
- Change bearings
- Add constraints

FREDPARRC

Analysis:

- Determine nominal loads during operation
- Determine infrequent loading
- Stress analysis on design solution



FREDPARRC

References:

- Previous literature on the machine design
- Patents
- Bell-Everman literature
- Kaydon/SKF catalogs
- ASM Material Catalog

FREDPARRC

| Risk | Countermeasure |
|--|--|
| Misalignment with extra constraints | No extra constraints. |
| Thermal degradation by convection | Better insulate the annealing kiln. |
| Thermal degradation by conduction through the shaft from the annealing | Thermally isolate the rotary stage with a low thermally conductive material. |

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Functional requirements – machine analysis

Analysis:

1. Extrusion/Drawing Forces
2. Operating Forces
3. Impact Forces
4. Human interaction

Limit = 200 N at the Build Plate

Extrusion at the Crucible

Governed by:

Bernoulli's
Equation

$$P_1 + \frac{1}{2}\rho v_1^2 + \rho gh_1 = P_2 + \frac{1}{2}\rho v_2^2 + \rho gh_2$$

Poiseuille's Law

$$P_2 - P_3 = \frac{8\mu LQ}{\pi R^4}$$

$F_{\text{extrude}} = 5 \text{ N}$

$$F = P_3 * \pi r_{\text{nozzle}}^2$$



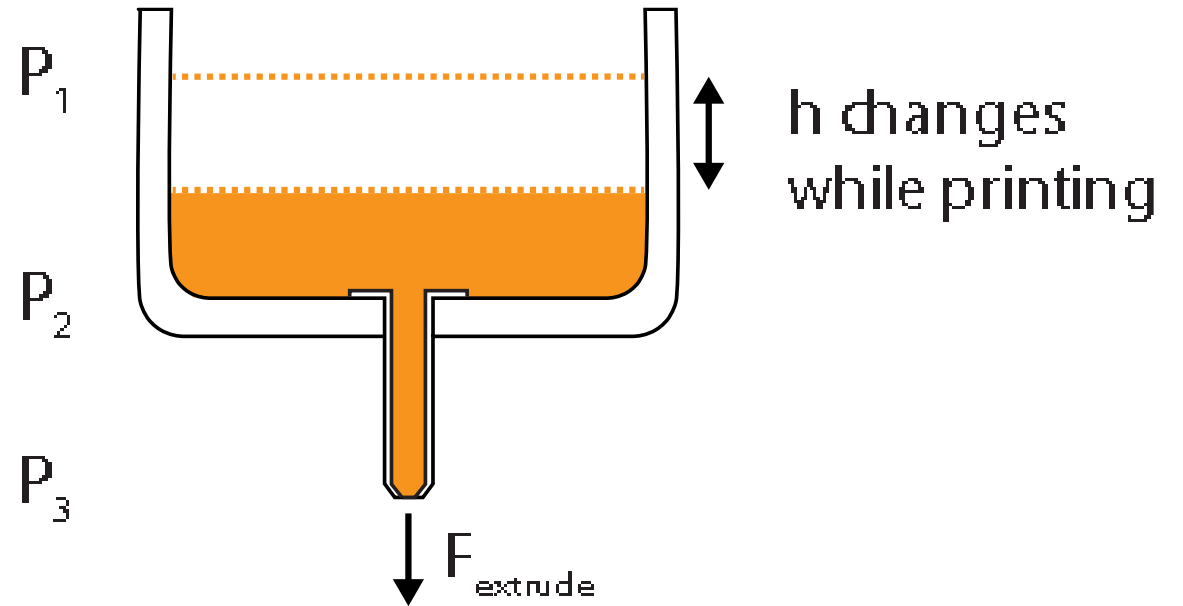
Glass



Bearings



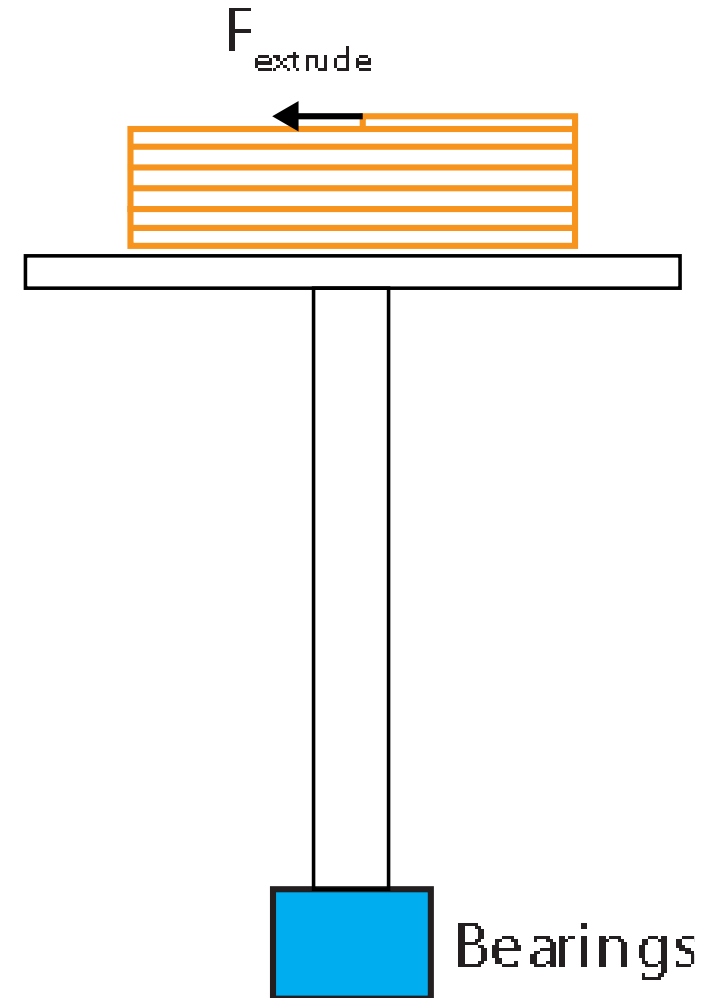
Printer Structure



Operating Forces

$$F_{\text{extrude}} = 5 \text{ N}$$

Far below bearing limits



Impact Force

Governed by:
Energy methods

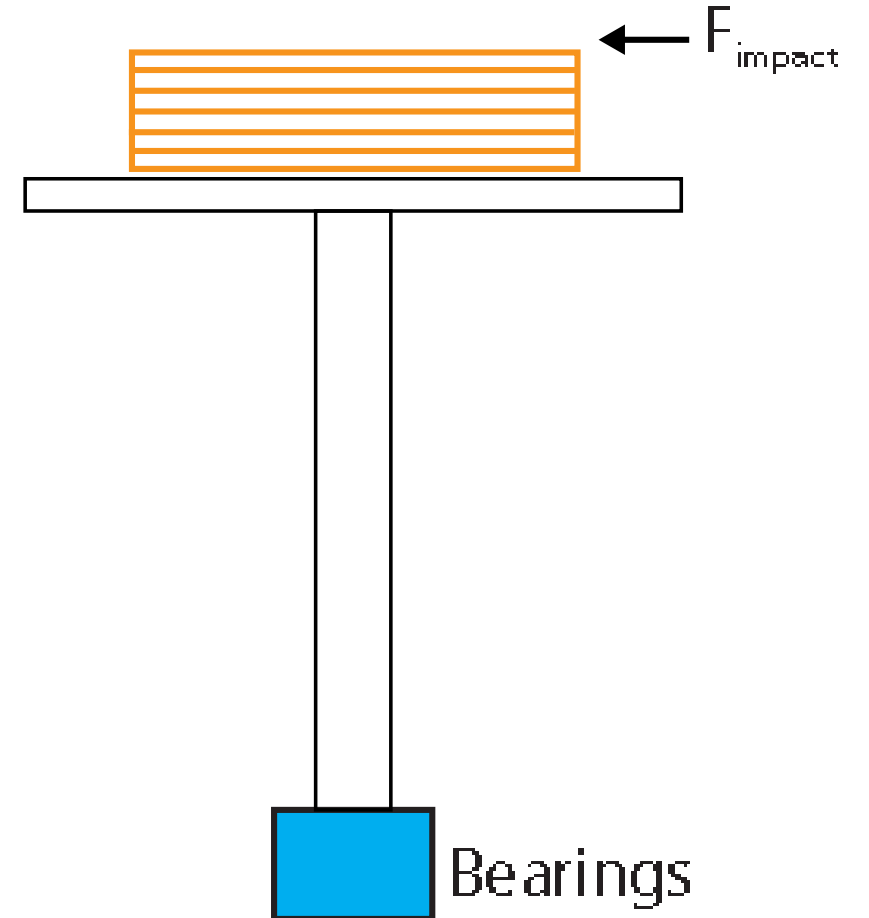
where k = stiffness of the
cantilevered beam

$$\frac{1}{2}mv^2 = \frac{1}{2}kx^2$$

$$x = \sqrt{\frac{1}{k}mv^2}$$

$$k = \frac{3EI}{L^3}$$

$$F_{\text{impact}} = kx = \sqrt{\frac{3EI}{L^3}mv^2}$$



Impact Force

Governed by:
Energy methods

where k = stiffness of the
cantilevered beam

$E = 193 \text{ GPa}$

$I = 5\text{E-}07 \text{ m}^4$

$L = 0.55 \text{ m}$

$m = 30 \text{ kg}$

$v = 0.01 \text{ m/s}$

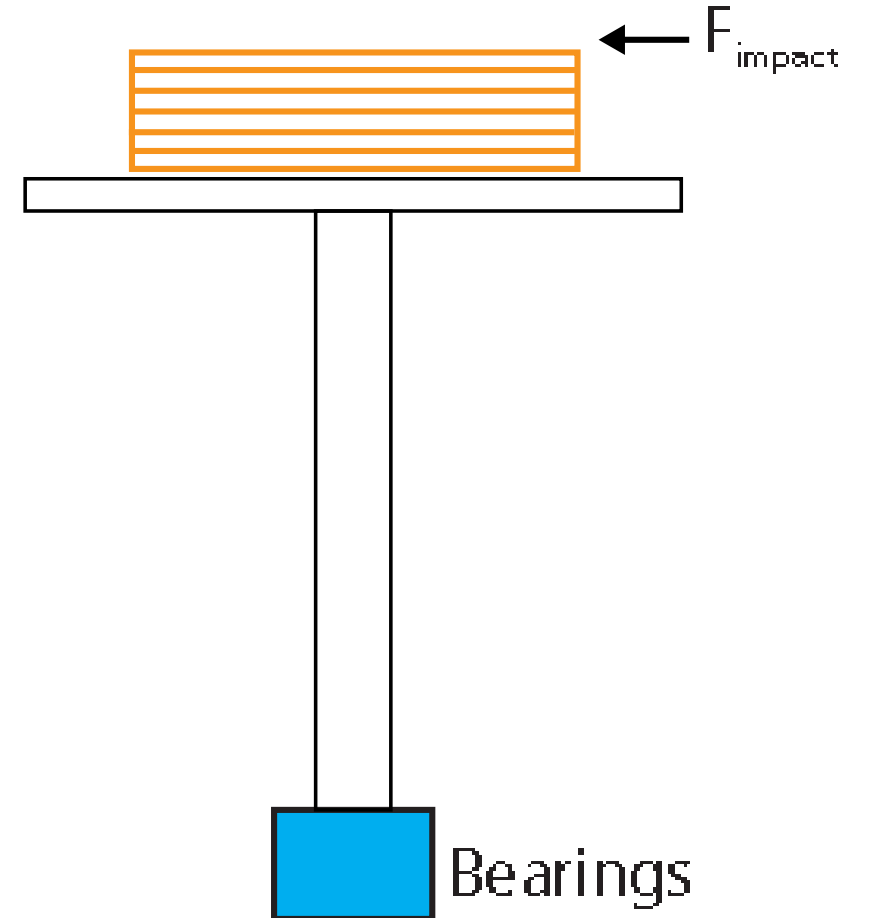
$F_{\text{impact}} \sim 70 \text{ N}$

$$\frac{1}{2}mv^2 = \frac{1}{2}kx^2$$

$$x = \sqrt{\frac{1}{k}mv^2}$$

$$k = \frac{3EI}{L^3}$$

$$F_{\text{impact}} = kx = \sqrt{\frac{3EI}{L^3}mv^2}$$



Force after Impact

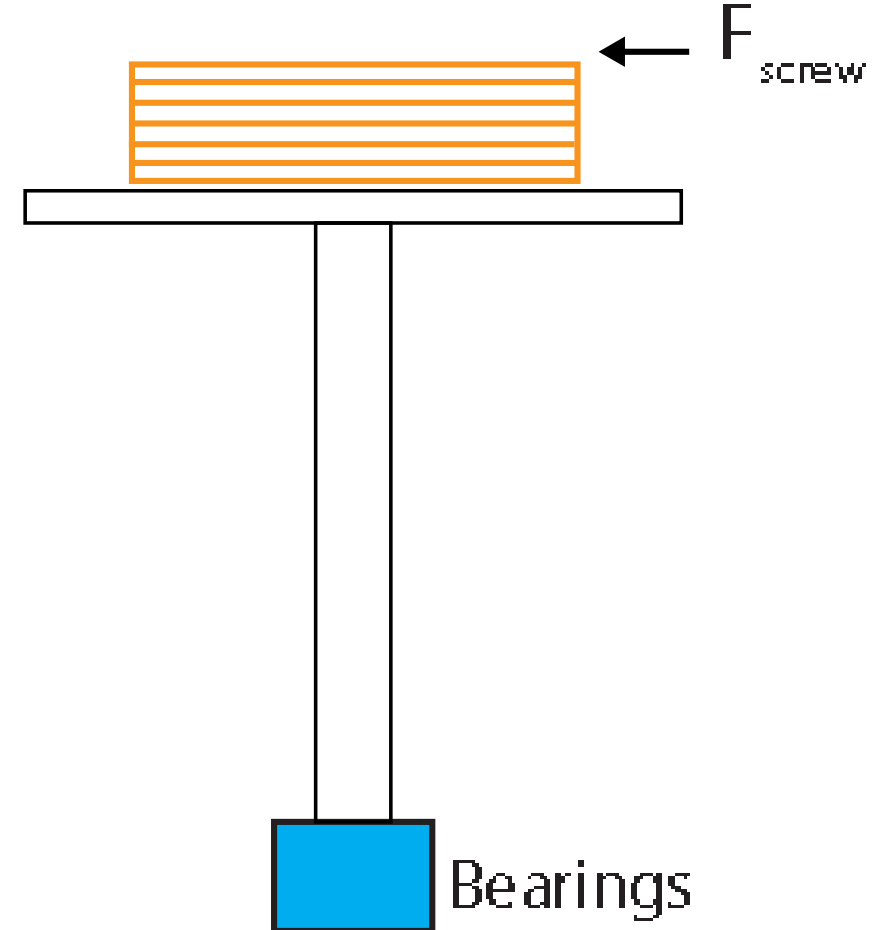
$$F_{screw} = \frac{2\pi\eta\tau}{l}$$

$$\eta = 0.9$$

$$\tau = 5.85 \text{ Nm}$$

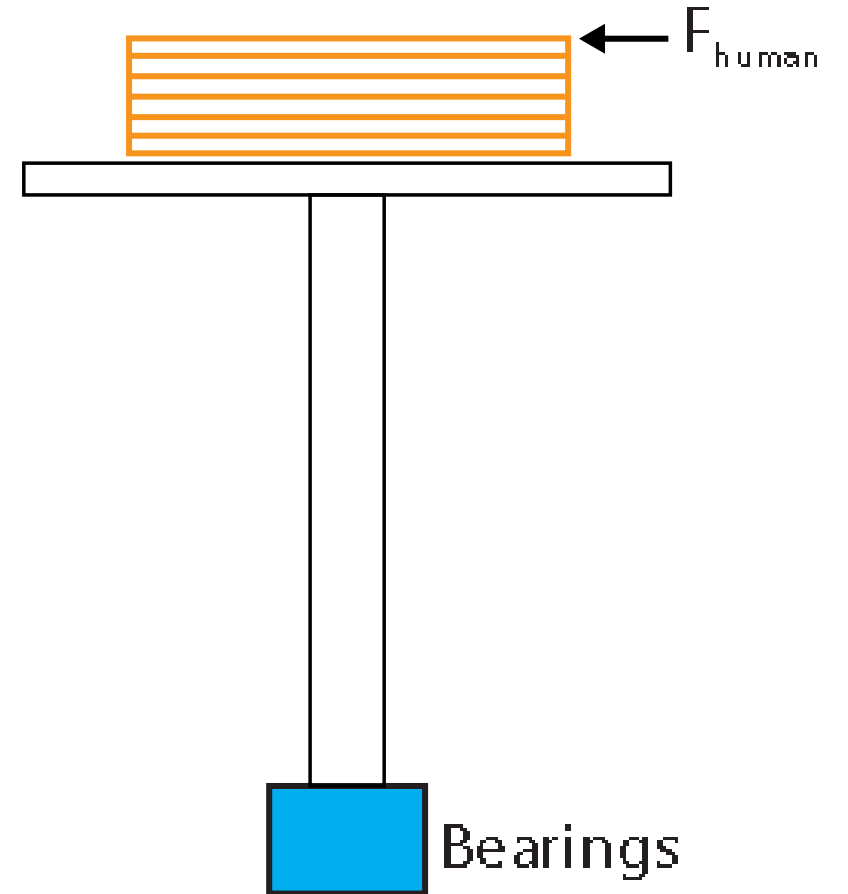
$$l = 20 \text{ mm}$$

$$F_{screw} = 496 \text{ N} = \text{Big Problem!}$$



Human Interaction

$$F_{\text{human}} = 534 \text{ N}_1$$



Functional requirements – summarized

Analysis:

1. Extrusion/Drawing Forces
2. Operating Forces
3. Impact Forces = 496 N
4. Human interaction = 534 N

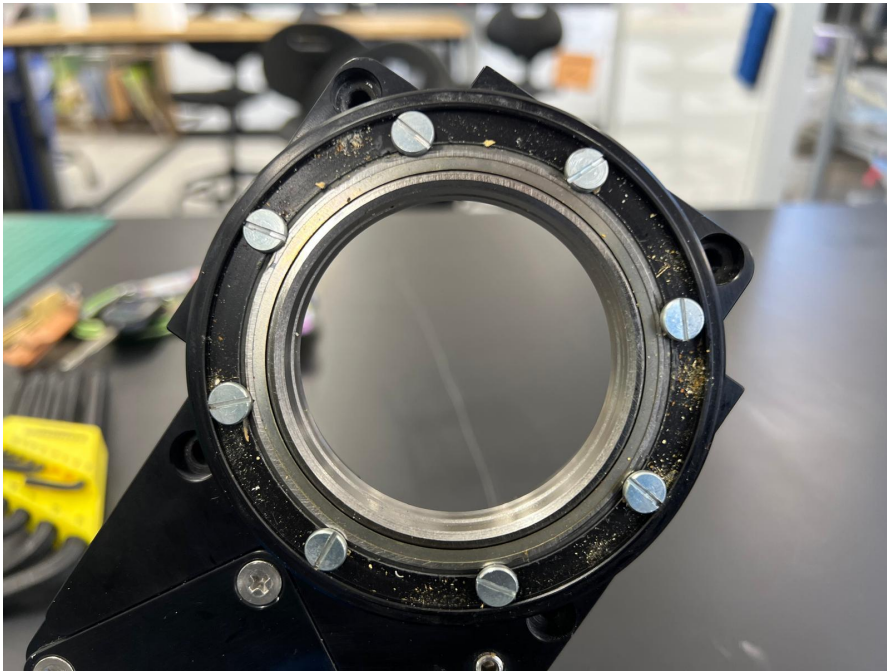
Limit = 200 N at the Build Plate

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Initial prediction – bearing failure

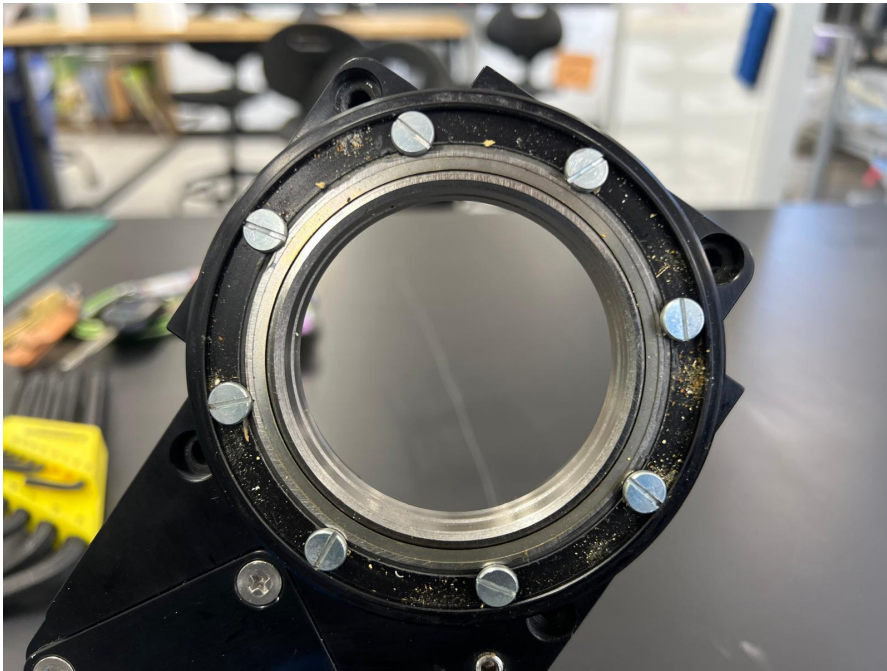
Analysis showed bearings
may have been overloaded



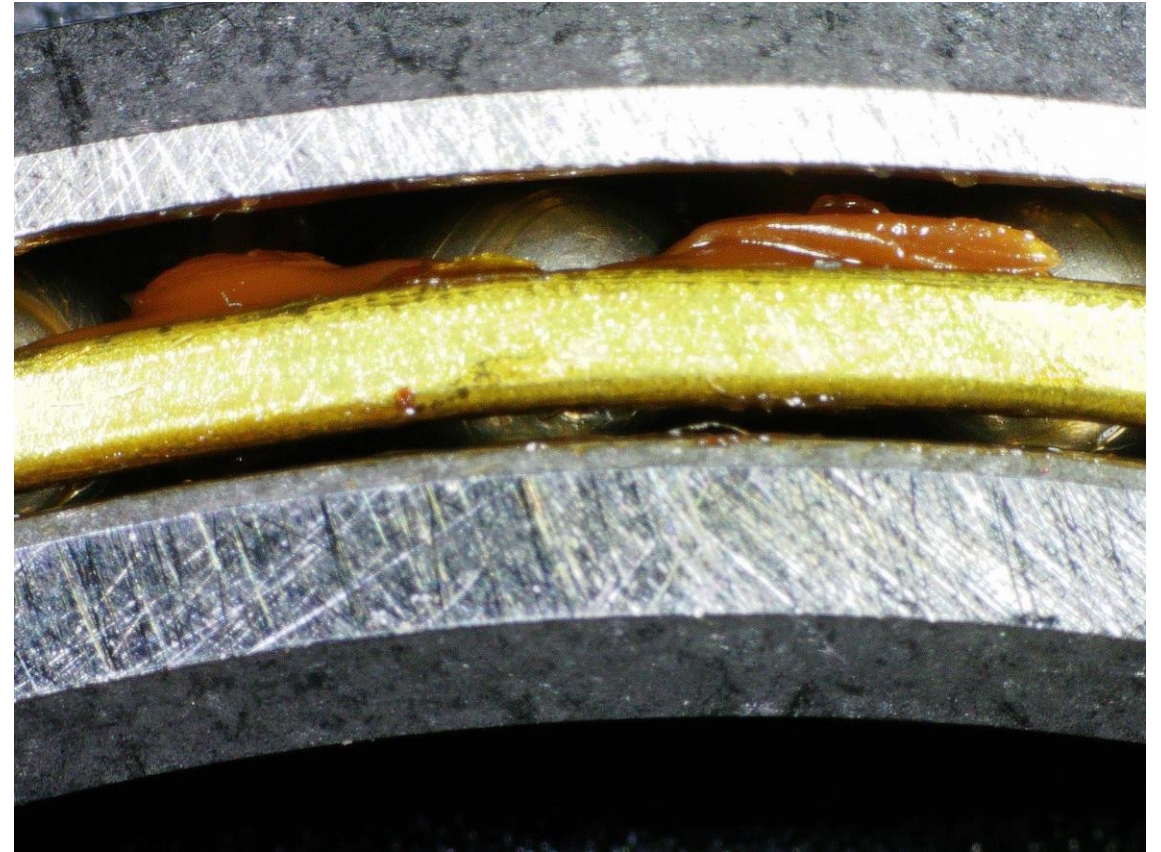
SBR-50 Rotary Stage Bearings

Initial prediction – bearing failure

Analysis showed bearings may have been overloaded



SBR-50 Rotary Stage Bearings

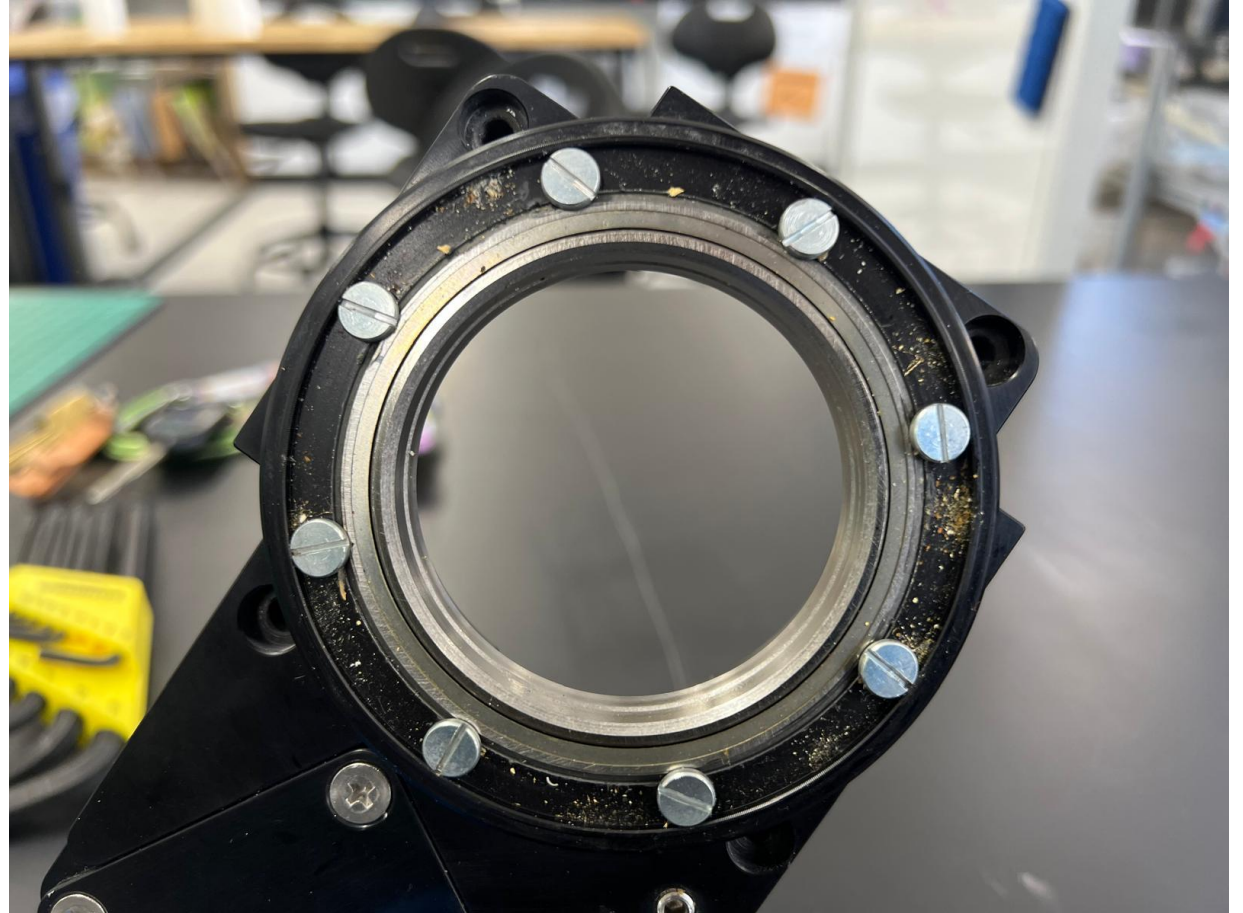


Bearings under magnification

Bearings did not show signs of damage



SBR-50 Rotary Table



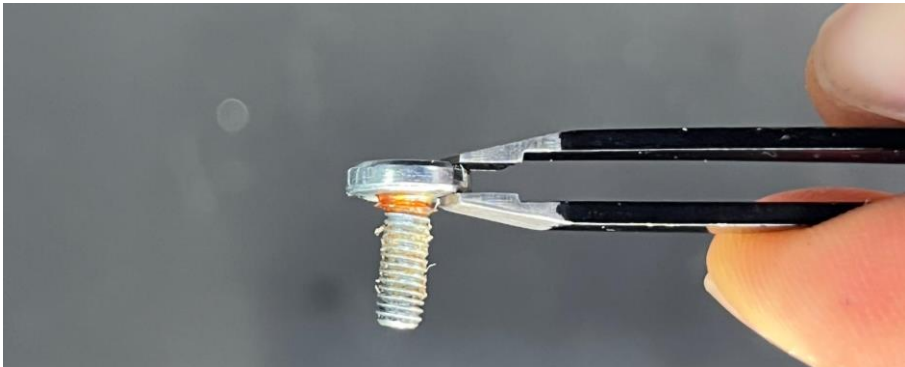
SBR-50 Rotary Table – constraint issue

Screws are directly bearing
on the outer race

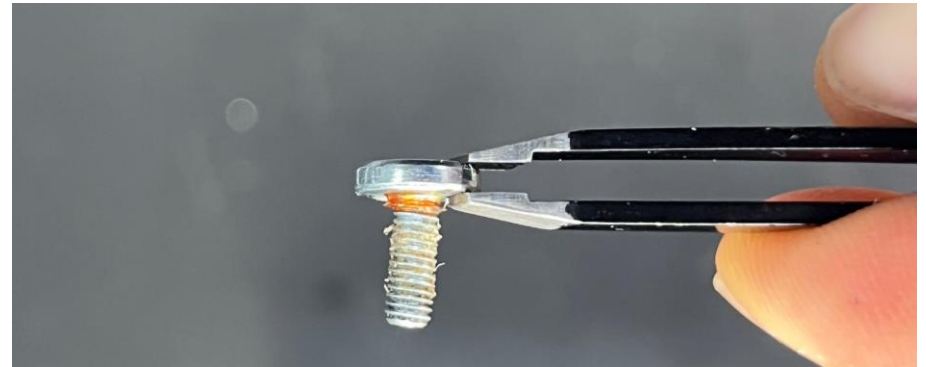
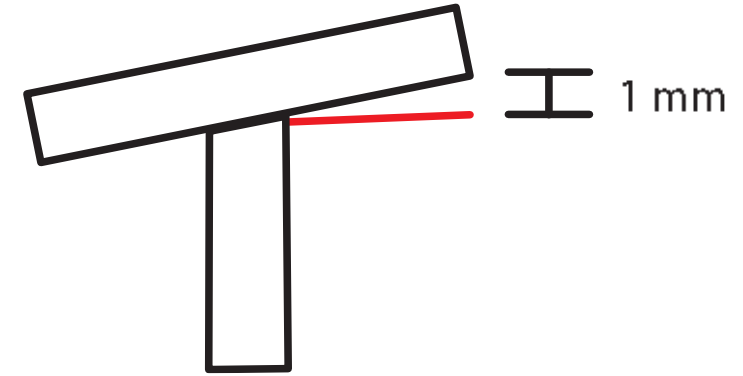


Outer constraint plastically deformed

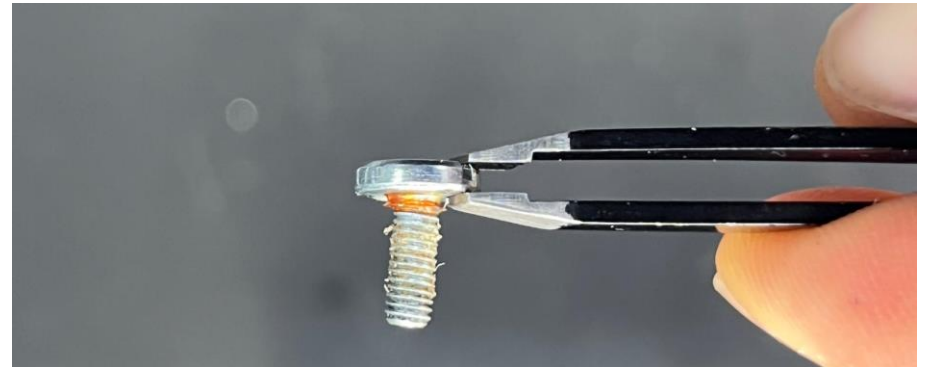
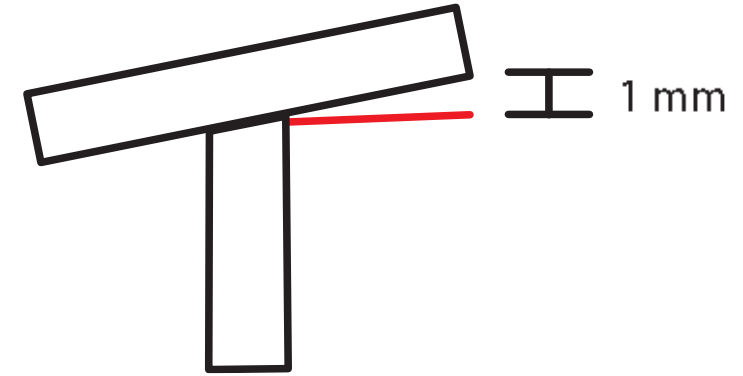
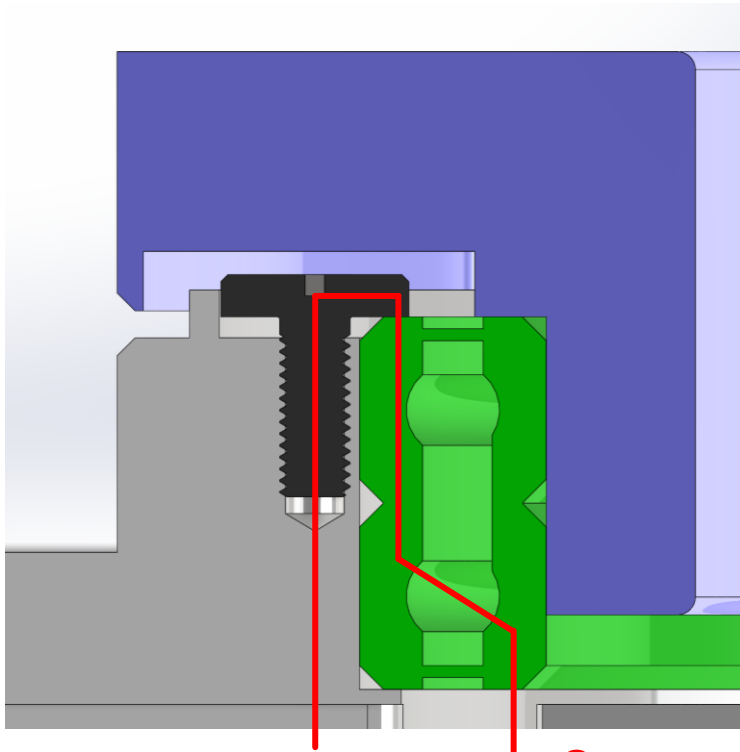
Screws are directly bearing on the outer race



Bent constraint from large moment



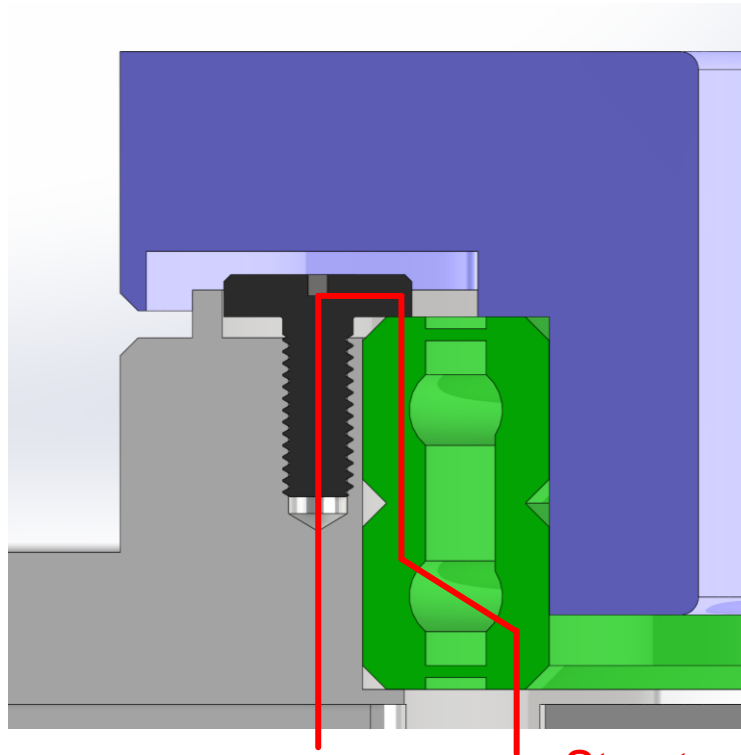
Bent constraint from large moment



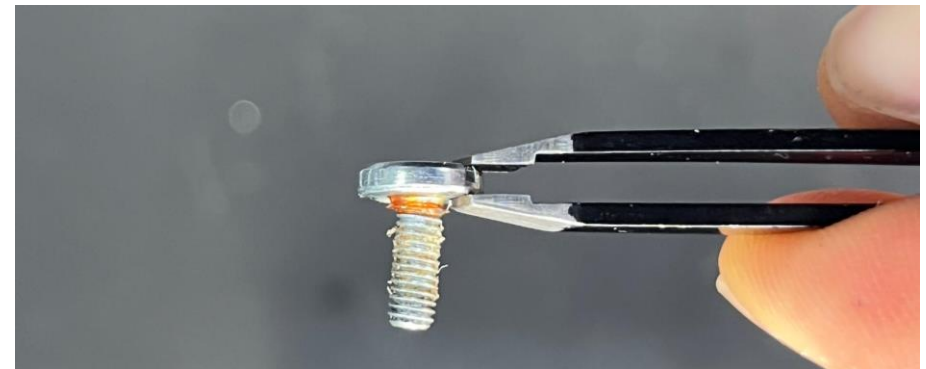
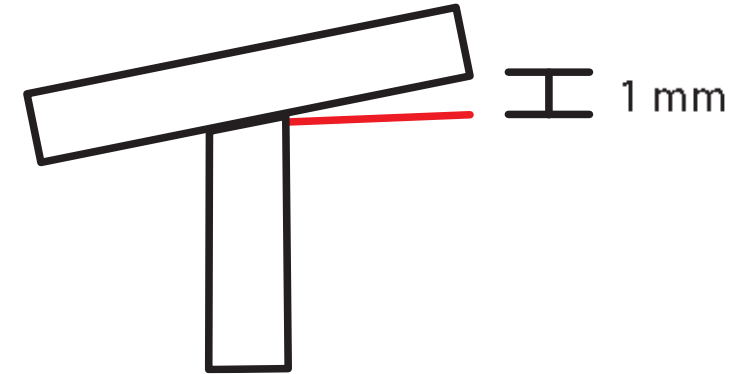
Structural Loop

Bent constraint from large moment

Bearings are unconstrained on outer races



Structural Loop



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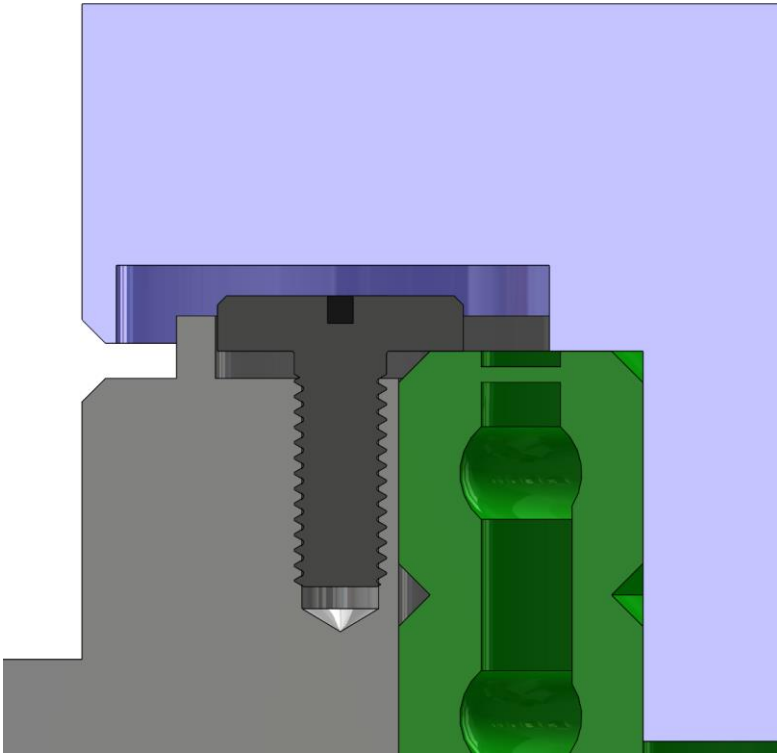
2 Design Strategies

1. Set motor torque limits to avoid impact overload
2. New outer race constraint to improve stiffness

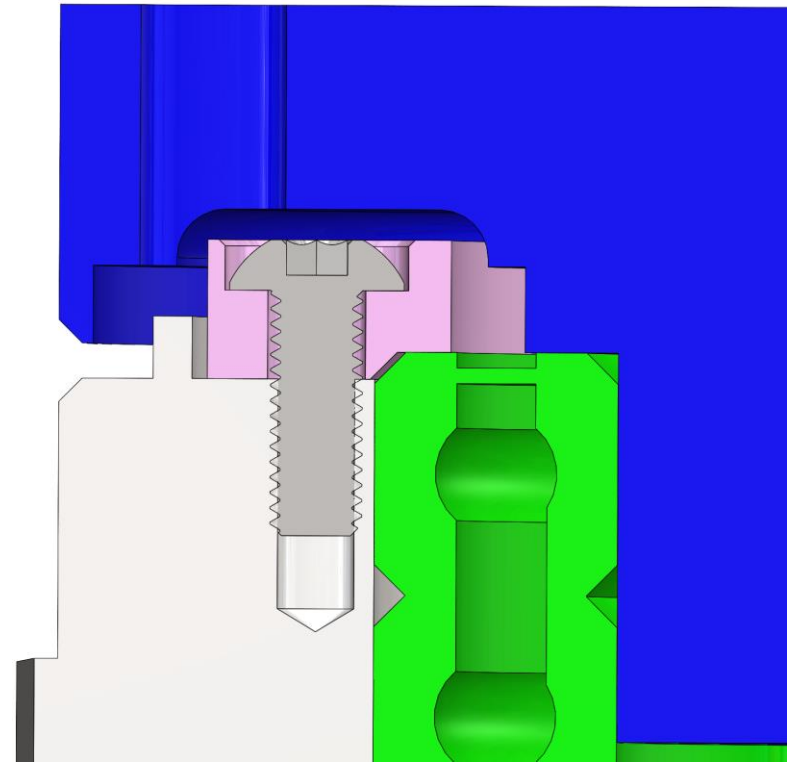
2 Design Strategies

1. Set motor torque limits to avoid impact overload
2. New outer race constraint to improve stiffness

Design strategy – new outer race constraint (pink)



Old Design



New Design

Design constraints and sizing

Analysis:

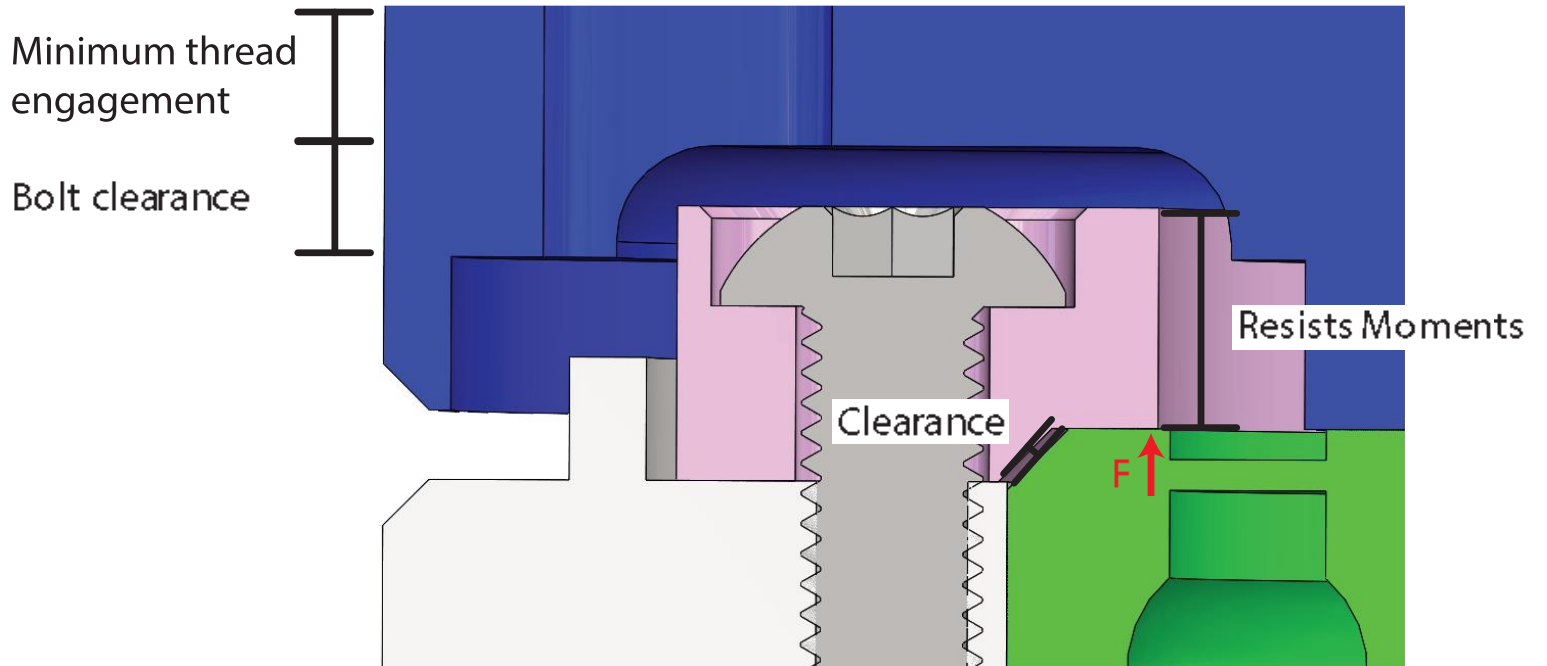
1. Clearance

a) Tolerance analysis

2. Resists moments

a) Cantilever beam

b) FEA



Design constraints and sizing

Analysis:

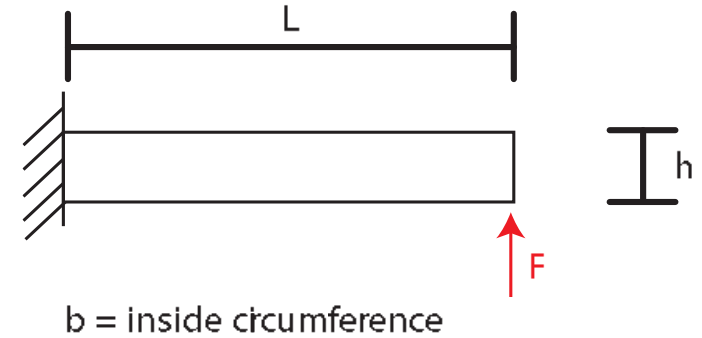
1. Clearance

a) Tolerance analysis

2. Resists moments

a) Cantilever beam

b) FEA



$$M = F * L$$

$$I = \frac{bh^3}{12}$$

$$\sigma_{max} = \frac{My}{I}$$

$$\sigma_{max} < \sigma_{yield}$$

Design constraints and sizing

Analysis:

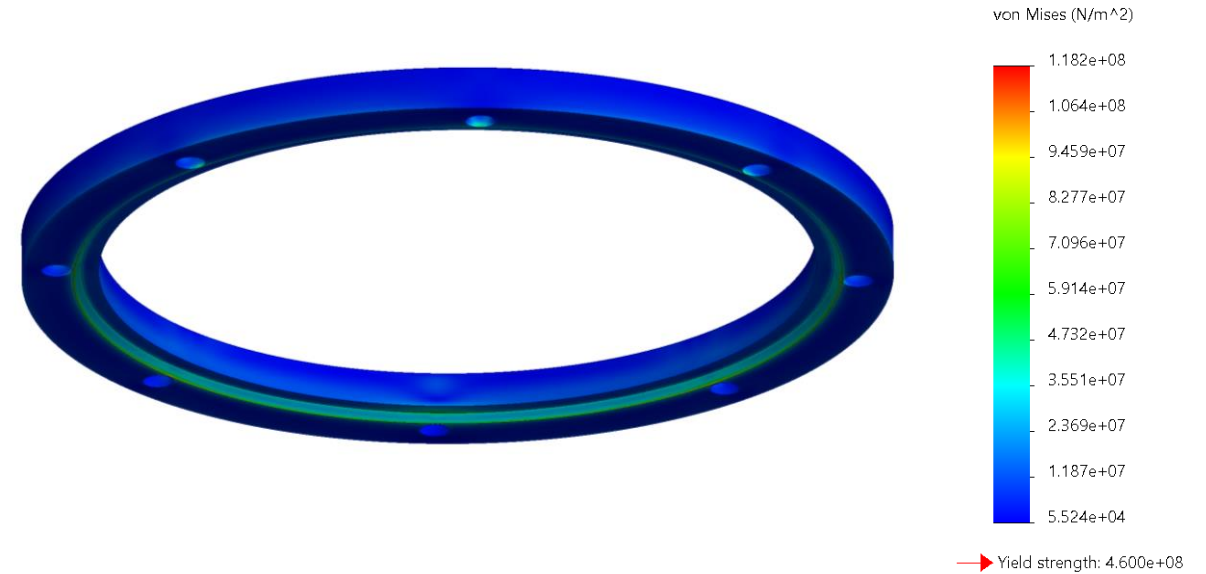
1. Clearance

a) Tolerance analysis

2. Resists moments

a) Cantilever beam

b) FEA – 4140 Steel



Final Results

Initially:

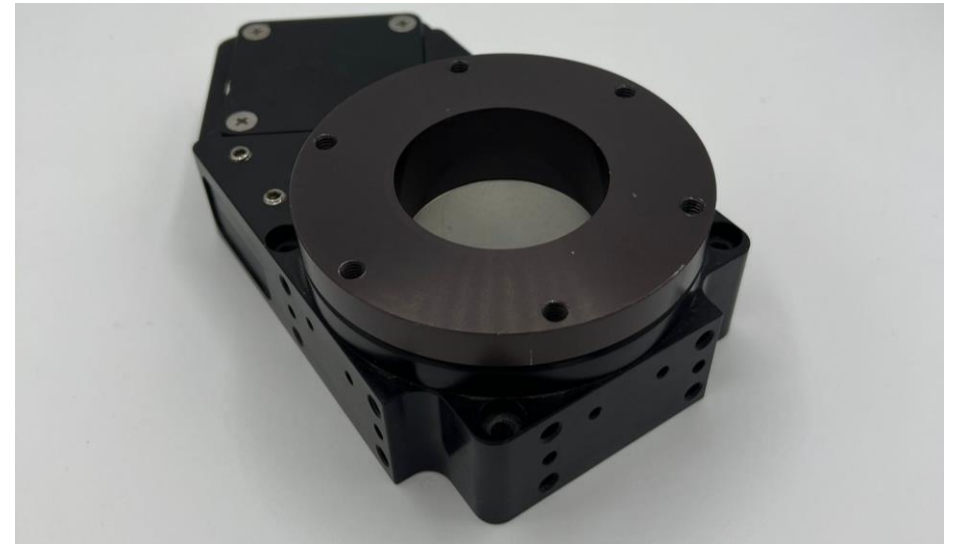
17 mm deflection at the build plate

Now:

Measured Stiffness = 1600 Nm/rad

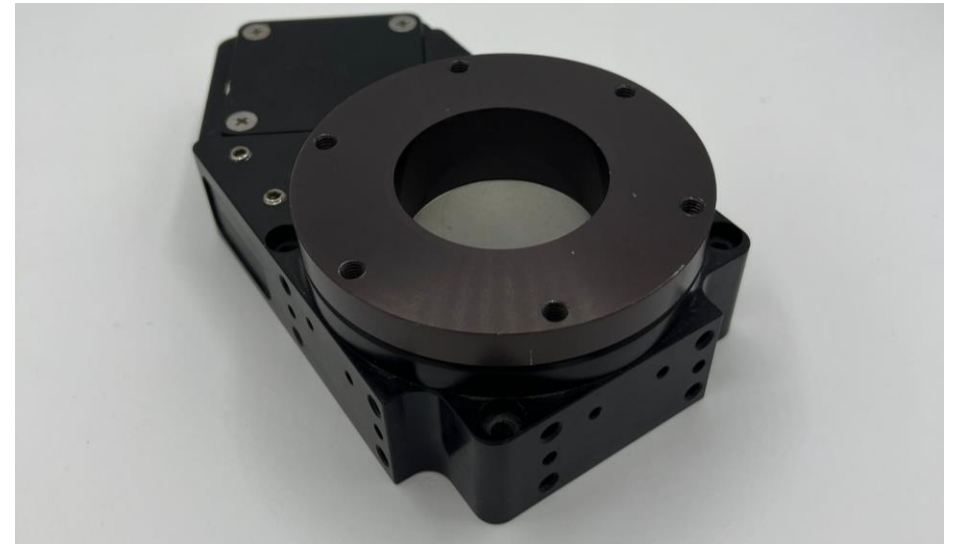
Predicted Stiffness = 4700 Nm/rad

Calculated deflection at the build plate = 1 mm



Next Steps

1. Increase stiffness to predicted value
 - Reseat the bearings as recommended by SKF
2. Continue working on mass measurement system





Thank you!

Fundamentals

- Abbe Errors
- Saint Venant's
- Structural Loop
- $F=kx$

Backup

Outer race lack of damage



Measuring Stiffness



Measuring Dimensions



Machining

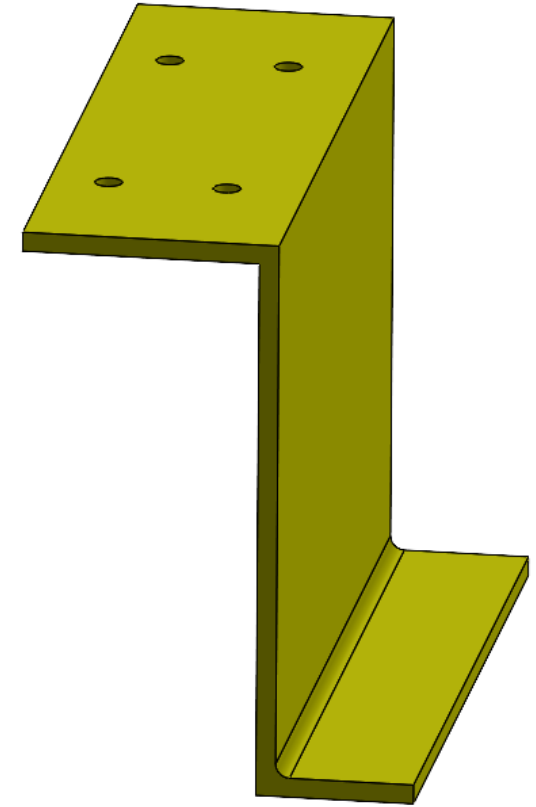


Kinematic Mount for crucible

Kelvin Kinematic Design

Ball size = 1" Diameter tool steel (Bal-Tec)

Groove Material = 6061 Aluminum



Design constraints and sizing

Analysis:

1. Clearance

a) Tolerance analysis

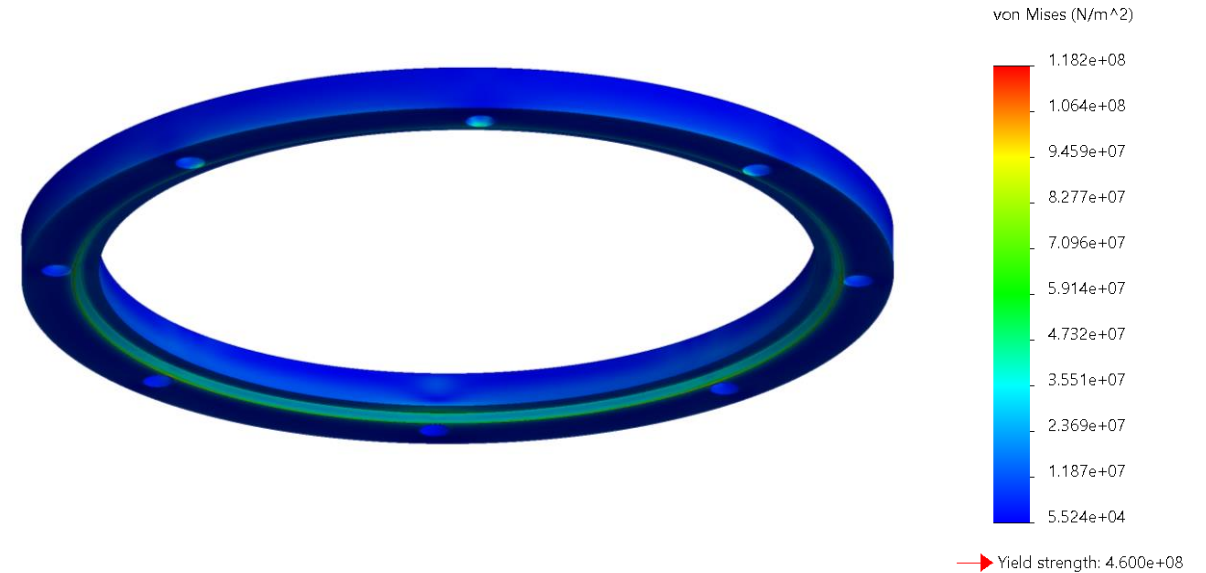
2. Resists moments

a) Cantilever beam

b) FEA – 4140 Steel

a) Stiffness: 4064 Nm/rad

b) Max Stress: 120 MPa



SKF Solution Code

Symptom D: Excessive shaft movement

| Possible cause | Solution code |
|----------------|---------------|
|----------------|---------------|

Looseness

- | | |
|---|----|
| • Inner ring loose on the shaft | 30 |
| • Outer ring excessively loose in the housing | 31 |
| • Bearing not properly clamped on the shaft or in the housing | 32 |

Surface damage

- | | |
|--|------------|
| • Wear from ineffective lubrication | 1, 2, 3, 4 |
| • Spalls in raceways and/or rolling elements due to fatigue | 37 |
| • Spalls in raceways and/or rolling elements due to surface initiated damage | 38 |

Incorrect internal bearing clearance

- | | |
|--|----|
| • Bearing with wrong clearance installed | 11 |
| • Bearing not properly clamped on the shaft or in the housing, excessive endplay | 33 |

SKF Solution Code

Outer ring creeps (turns) in the housing seat

Worn or oversized seat

Considerations about fits or creep:

- Most applications have a stationary housing where the load is unidirectional. This is considered a stationary outer ring load and, under most conditions, the outer ring can be held in place with a loose fit.
- However, an outer ring can creep or turn in its housing seat if the seat is oversized or worn.
- This leads to increased noise and vibration levels as well as wear.

Actions:

- Metalize and regrind the housing seat to the appropriate size.
- For large housings, machining the seat to a larger diameter and using a cartridge sleeve might be a solution.

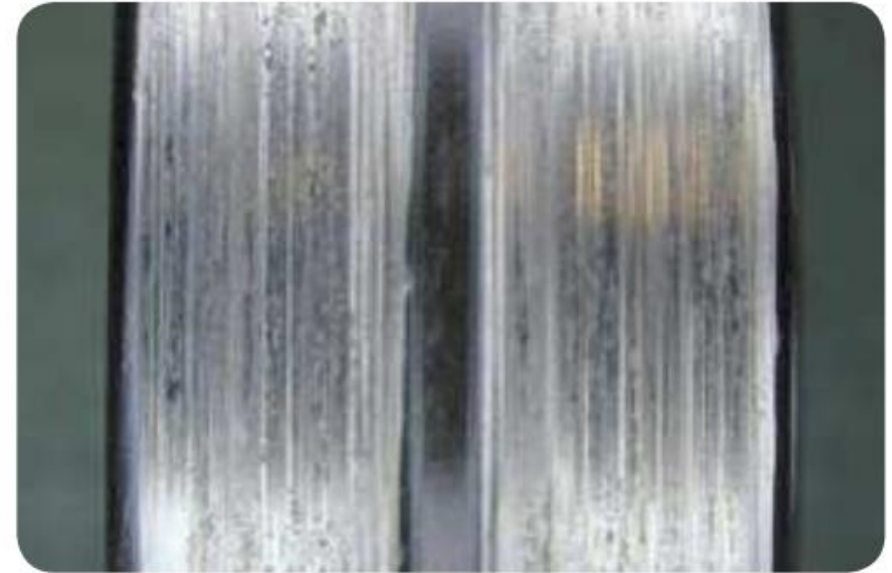
Unbalanced load

Considerations about fits or creep:

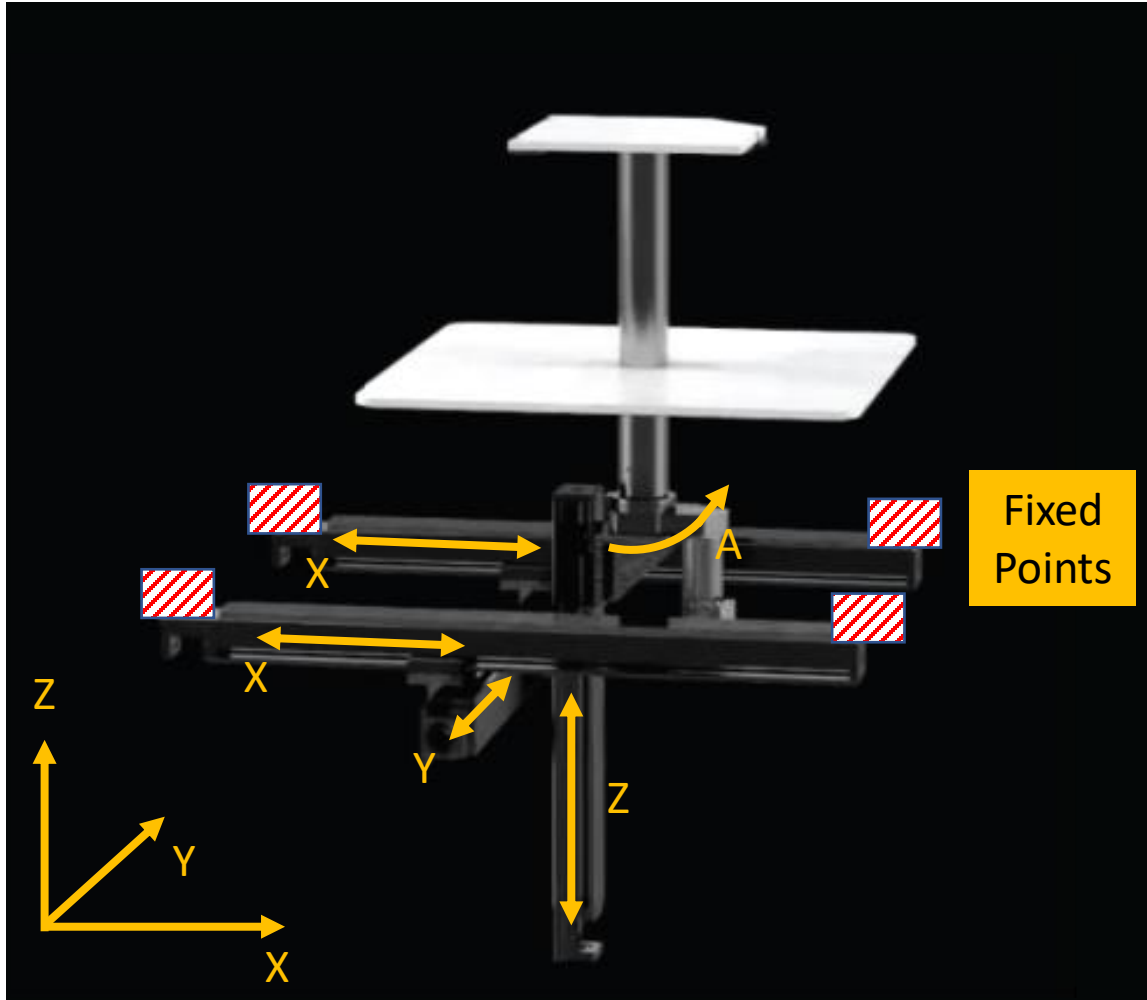
- Loads resulting from an unbalanced shaft can cause outer ring creep, even if the fits are correct.

Actions:

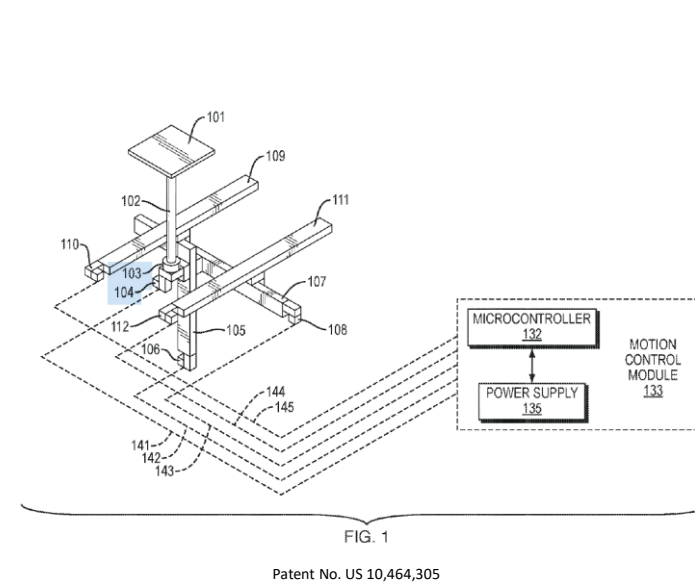
- Eliminate the source of the unbalance.
- Rebalance the machine.



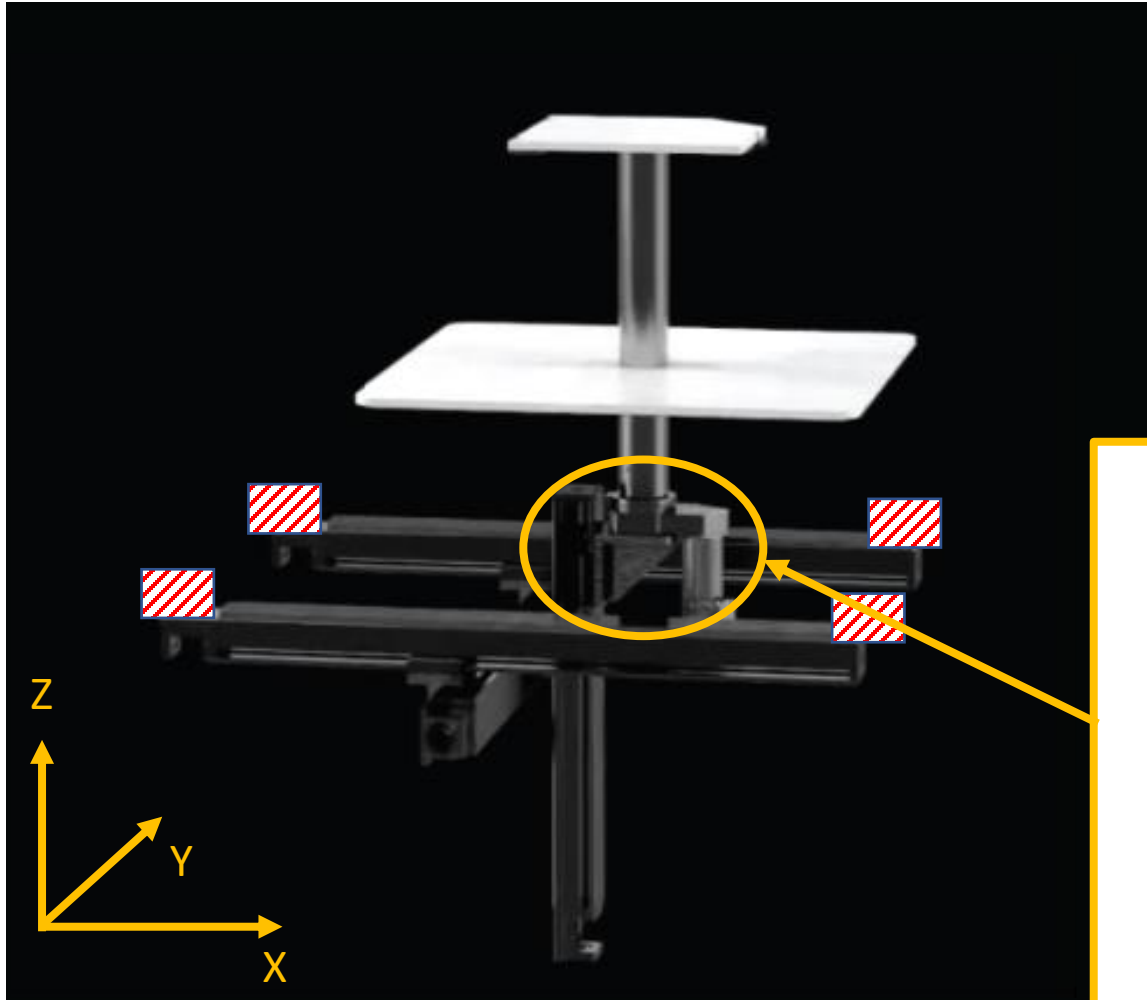
CNC Frame – Motion



<https://oxman.com/projects/glass-ii>



CNC Frame – Rotary Axis



<https://oxman.com/projects/glass-ii>

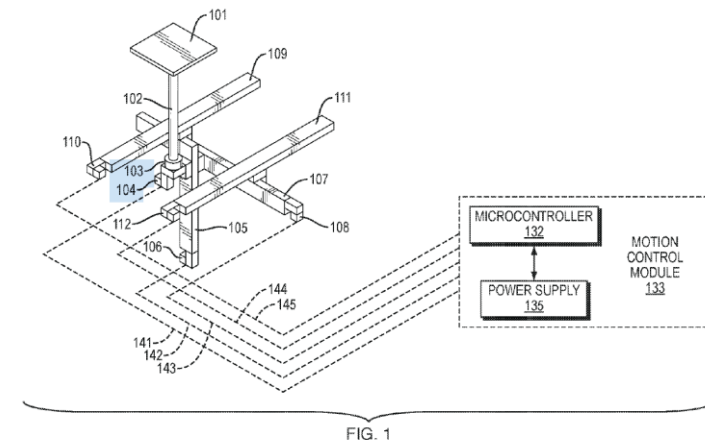


FIG. 1
Patent No. US 10,464,305

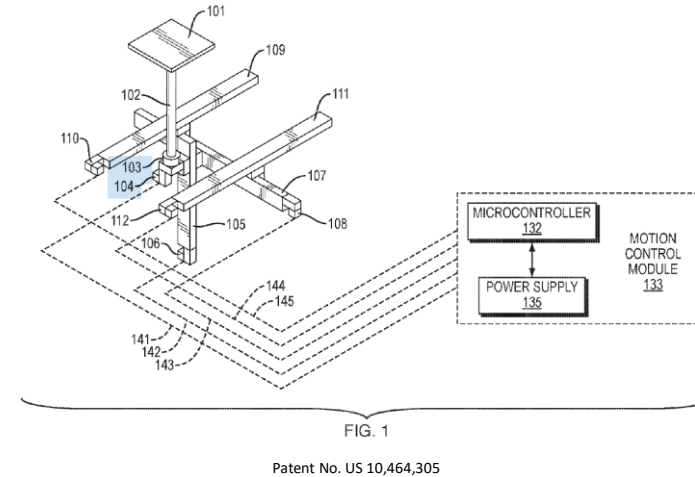
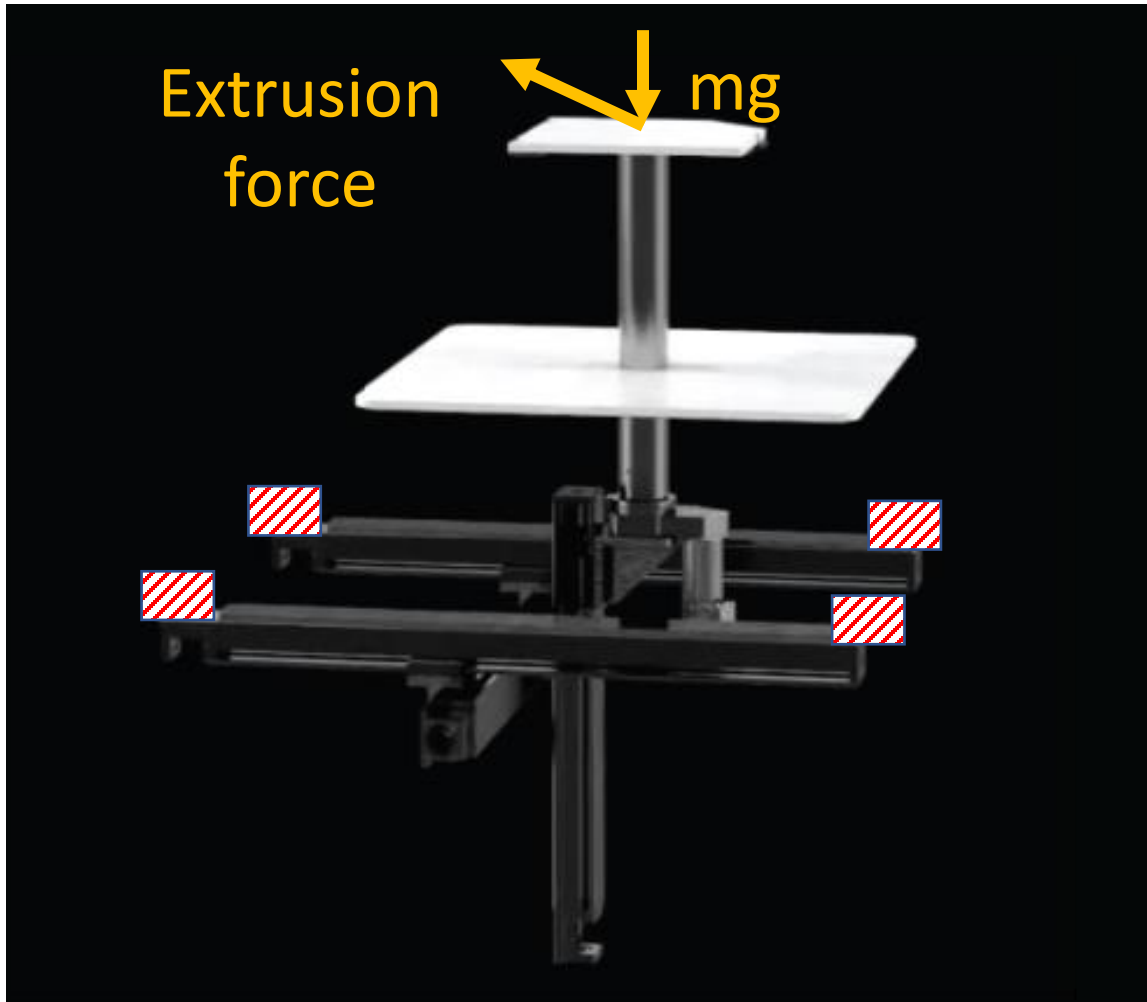


“large full duplex,
angular contact
bearings”

Bell-Everman SBR-50 Rotary Table

<https://www.bell-everman.com/products/rotary-positioning/servobelt-rotary-stage>

Topic 2 – Statics FBD



2. Integrate sensors to:

- Measure the weight of the extruded material
- Measure lateral loads and torques on z-shaft



Topics Summarized

1. Devise a new connection to Z-drive to:
 - a. Avoid overloading the bearings of the rotary stage
 - b. Improve stiffness
2. Integrate sensors to:
 - a. Measure the weight of the extruded material
 - b. Measure lateral loads and torques on the z-shaft